Algorithmic computation of groups of equivariant homotopy classes of maps

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I will outline an algorithm for the computation of the set $[X, Y]^A$ of Gequivariant homotopy classes of maps $X \to Y$ extending a given map $A \to Y$ defined on a subsapce $A \subseteq X$ (simply connected Y, finite G); this algorithm works under a certain "stability assumption", defined by the requirement dim $X^H \leq 2 \cdot \operatorname{conn} Y^H$ on the dimension and the connectivity of the fixed point sets for all subgroups $H \leq G$.

(When the stability assumption is dropped – but Y is still assumed simply connected – it is already impossible to decide if $[X, Y]^A$ is non-empty; this is a result of our previous work that I will also try to briefly summarize.)